## 2019 INTERNATIONAL ENGINEERING MECHANICS CONTEST (ASIAN REGION) The Theory Contest

 thread makes an angle $\alpha$ with the plane.

## Problem K-2

The disk of radius $R$ rolls without sliding along a fixed plane. The velocity and the acceleration of the disk center at a given time are $v$ and $a$ respectively. The thread $\mathbf{A B}$ is wound on the disk. Determine the -velocity and the acceleration of the thread end $\mathbf{B}$ if the

## Problem S-1

A uniform heavy cylinder touches a vertical wall and it is held in the equilibrium by two horizontal cables $\mathbf{B D}$ and two weightless rods $\mathbf{A B}$ that are pivotally attached to the wall. At what value of the angle $\alpha$ the tension of the cables will be the minimal?

## Problem S-2

A thin homogeneous rod $\mathbf{A B}$ of length $2 r$ rests on a rough disk of radius $r$. The rod is held in balance by a weightless thread $\mathbf{C B}$ of length $r$. Determine the coordinates of the point $\mathbf{C}$ that is the attachment point of the thread, if the $\operatorname{rod} \mathbf{A B}$ is inclined to the horizontal and $\mathbf{B C}$ - to the vertical at an angle $\varphi$. The friction in the hinge can be neglected.

## Problem K-1

The rectangular plate moves in its plane with a constant angular velocity $\omega$. Determine the velocity and acceleration of the plate top $\mathbf{C}$ and of the plate point $\mathbf{K}$ that is the midpoint of the section $\mathbf{A B} . \mathbf{A B}=l$.

## Problem D-1



The loads 1, 2, 3 are connected by a weightless inextensible thread thrown over a block of radius $r$ and they have the same mass $m$. The dimensions of the loads can be neglected. The system starts to move without the initial velocity from the position shown in the figure. The dimensions $H$ and $l$ are given. At what maximal height will the load 3 rise, if the axial moment of inertia of the block is equal to $m r^{2}$, and the loads 1 and 2 remain stationary after reaching the floor?

## Problem D-2

A non-uniform disk of radius $r$ oscillates in a vertical plane around the axis $\mathbf{O}$. The density of the disk is proportional to the distance to the axis $\mathbf{C}$, passing through the center of the disk. Determine the period of small oscillations of the disk.

## Problem D-3

A rough uniform cylinder 1 and a thin pipe 2 of the same radii and masses, roll without slipping along a rough inclined plane forming an angle $\alpha$ with the horizon. The coefficient of sliding friction between the cylinders is $f$. Determine the acceleration of the centers of the cylinders of rolling bodies.

## Problem D-4

Four homogeneous rods of length $l$ and mass $m$ each are connected by hinges and form a square located on a smooth horizontal plane. The force $F$ was applied to a hinge $\mathbf{A}$ in the shown direction. Before the force application the system rested. Determine the hinge $\mathbf{A}$ acceleration at the initial movement moment.

